

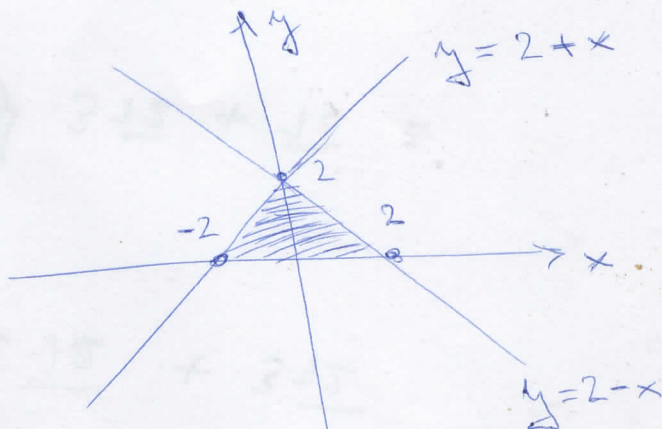
$$1. \iint_D (x+y)^3 dx dy \stackrel{\text{F.V.}}{=} \int_0^2 \int_{y-2}^{2-y} (x+y)^3 dx dy =$$

$$= \int_0^2 \left[\frac{(x+y)^4}{4} \right]_{y-2}^{2-y} dy$$

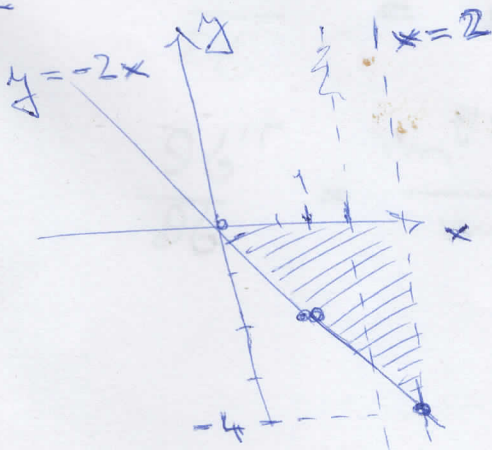
$$= \int_0^2 (16 - (2y-2)^4) dy$$

$$= \frac{1}{4} \cdot 16 \cdot \int_0^2 (1 - (y-1)^4) dy$$

$$= 4 \cdot \left[y - \frac{(y-1)^5}{5} \right]_0^2 = 4 \cdot \left(2 - \frac{1}{5} + \frac{1}{5} \right) = \underline{\underline{\frac{32}{5}}}$$



$$2. \int_{-4}^0 \left(\int_{-4}^{-2x} \cos\left(\frac{\pi y}{4x}\right) dx \right) dy \stackrel{\text{F.V.}}{=} \int_0^2 \int_{-2x}^0 \cos\frac{\pi y}{4x} dy dx =$$

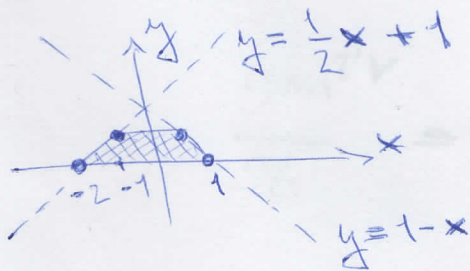


$$= \int_0^2 \left[\frac{4x}{\pi} \sin\frac{\pi y}{4x} \right]_{-2x}^0 dx$$

$$= \int_0^2 \frac{4x}{\pi} \cdot \left(\underbrace{\sin 0}_0 - \underbrace{\sin\left(-\frac{\pi}{2}\right)}_{-1} \right) dx$$

$$= \frac{4}{\pi} \int_0^2 x dx = \frac{4}{\pi} \left[\frac{x^2}{2} \right]_0^2 = \underline{\underline{\frac{8}{\pi}}}$$

3.



$$\int_0^{1/2} \int_{2y-2}^{1-y} \frac{1}{1-y} dx dy =$$

$$= \int_0^{1/2} \frac{1-y - (2y-2)}{1-y} dy = \int_0^{1/2} \frac{-3y+3}{1-y} dy = \int_0^{1/2} 3 dy = \underline{\underline{\frac{3}{2}}}$$